

# HEMCHAND YADAV VISHWAVIDYALAYA, DURG (C.G.)

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## SCHEME OF EXAMINATION & SYLLABUS of M.A./M.Sc.(Mathematics) Semester Exam UNDER FACULTY OF SCIENCE Session 2019-20

(Approved by Board of Studies)  
Effective from June 2019

M.A./M.Sc. (MATHEMATICS)  
(Semester-I) 2019-20

There shall be five papers. Each paper shall have 100 marks. **Overall tally of marks will be 500.**

Paper	Description	Theory	Sessional	Practical	Total Marks
I	Advanced Abstract Algebra (I)	80	20	-	100
II	Real Analysis (I)	80	20	--	100
III	Topology	80	20	--	100
IV	Advanced Complex Analysis (I)	80	20	--	100
V	Advanced Discrete Mathematics (I)	80	20	--	100

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# HEMCHAND YADAV VISHWA VIDYALAYA, DURG (C.G.)

## M.Sc./M.A. Course (First Semester)

### PAPER -I

## Advanced Abstract Algebra (I)

Max. Marks 80

- Unit-I** Groups - Normal and Subnormal series. Composition series. Jordan-Holder theorem. Solvable groups. Nilpotent groups.
- Unit-II** Field theory- Extension fields. Algebraic and transcendental extensions. Separable and inseparable extensions. Algebraically closed fields.
- Unit-III** Perfect fields. Finite fields. Primitive elements. Normal extensions, Splitting field.
- Unit-IV** Automorphisms of extensions. Galois extensions. Fundamental theorem of Galois theory.
- Unit-V** Solution of polynomial equations by radicals. Insolvability of the general equation of degree 5 by radicals.

### Books Recommended:

1. P. B. Bhattacharya, S. K. Jain, S. R. Nagpaul: Basic Abstract Algebra, Cambridge University press
2. I. N. Herstein: Topics in Algebra, Wiley Eastern Ltd.
3. Vivek Sahai and Vikas Bist: Algebra, Narosa Publishing House, 1999.

### References

1. M. Artin, Algebra, Prentice -Hall of India, 1991.
2. P. M. Cohn, Algebra, Vols. I, II & III, John Wiley & Sons, 1982, 1989, 1991.
3. N. Jacobson, Basic Algebra, Vols. I, W.H. Freeman, 1980 (also published by Hindustan Publishing Company).
4. S. Lang, Algebra, 3rd edition, Addison-Wesley, 1993.
5. I. S. Luther and I. B. S. Passi, Algebra, Vol. I-Groups, Vol. II-Rings, Narosa Publishing House (Vol. I-1996, Vol. II-1999)
6. D. S. Malik, J. N. Mordeson, and M. K. Sen, Fundamentals of Abstract Algebra, Mc Graw-Hill, International Edition, 1997.
7. Qazi Zameeruddin and Surjeet Singh : Modern Algebra
8. I. Stewart, Galois theory, 2nd edition, Chapman and Hall, 1989.
9. J. P. Escofier, Galois theory, GTM Vol.204, Springer, 2001..
10. Fraleigh , A first course in Algebra Algebra, Narosa, 1982.



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# M.Sc./M.A. Course (First Semester)

## PAPER-II

### Real Analysis (I)

Max. Marks 80

**Unit-I** Sequences and series of functions, pointwise and uniform convergence, Cauchy criterion for uniform convergence, Weierstrass M-test, Abel's and Dirichlet's tests for uniform convergence, uniform convergence and continuity, definition and simple properties of Riemann-Stieltjes integral, uniform convergence and Riemann-Stieltjes integration, uniform convergence and differentiation, Weierstrass approximation theorem.

**Unit-II** Power series, uniqueness theorem for power series, Abel's and Tauber's theorems. Rearrangements of terms of a series, Riemann's theorem.

**Unit-III** Functions of several variables, linear transformations, Derivatives in an open subset of  $\mathbb{R}^n$ , Chain rule, Partial derivatives, interchange of the order of differentiation, Derivatives of higher orders, Taylor's theorem, Inverse function theorem, Implicit function theorem.

**Unit-IV** Jacobians, extremum problems with constraints, Lagrange's multiplier method, Differentiation of integrals.

**Unit-V** Partitions of unity, Differential forms, Stoke's theorem.

#### Recommended Books:

1. Principle of Mathematical Analysis by Walter Rudin (3rd edition) McGraw-Hill, Kogakusha, 1976, International student edition.
2. Real Analysis by H. L. Roydon, Macmillan Pub. Co. Inc. 4th Edition, New York .1962.



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## References

1. T. M. Apostol, Mathematical Analysis, Narosa Publishing House, New Delhi, 1985.
2. Gabriel Klambauer, Mathematical Analysis, Marcel Dekkar, Inc. New York, 1975.
3. A. J. White, Real Analysis; an introduction, Addison-Wesley Publishing Co., Inc., 1968.
4. G. de Barra, Measure Theory and Integration, Wiley Eastern Limited, 1981.
5. E. Hewitt and K. Stromberg. Real and Abstract Analysis, Berlin, Springer, 1969.
6. P. K. Jain and V.P. Gupta, Lebesgue Measure and Integration, New Age International (P) Limited Published, New Delhi, 1986 Reprint 2000).
7. I. P. Natanson, Theory of Functions of a Real Variable. Vol. I, Frederick Ungar Publishing Co., 1961.
8. Richard L. Wheeden and Antoni Zygmund, Measure and Integral: An Introduction to Real Analysis, Marcel Dekker Inc. 1977.
9. J. H. Williamson, Lebesgue Integration, Holt Rinehart and Winston, Inc. New York. 1962.
10. A. Friedman, Foundations of Modern Analysis, Holt, Rinehart and Winston, Inc., New York, 1970.
11. P. R. Halmos, Measure Theory, Van Nostrand, Princeton, 1950.
12. T. G. Hawkins, Lebesgue's Theory, of Integration: Its Origins and Development, Chelsea, New York, 1979.
13. K. R. Parthasarathy, Introduction to Probability and Measure, Macmillan Company of India Ltd., Delhi, 1977.
14. R. G. Bartle, The Elements of Integration, John Wiley & Sons, Inc. New York, 1966.
15. Serge Lang, Analysis I & II, Addison-Wesley Publishing Company, Inc. 1969.
16. Inder K. Rana, An Introduction to Measure and Integration, Norosa Publishing House, Delhi, 1997.
17. Walter Rudin, Real & Complex Analysis, Tata McGraw-Hill Publishing Co. Ltd. New Delhi, 1966.



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# M.Sc./M.A. Course (First Semester)

## PAPER-III

### Topology

Max. Marks 80

**Unit-I** Countable and uncountable sets. Infinite sets and the Axiom of Choice. Cardinal numbers and its arithmetic. Schroeder-Bernstein theorem. Cantor's theorem and the continuum hypothesis. Zorn's lemma, well-ordering theorem. Definition and examples of topological spaces. Closed sets. Closure. Dense subsets. Neighbourhoods. Interior, exterior and boundary. Accumulation points and derived sets. Bases and sub-bases. Subspaces and relative topology.

**Unit-II** Alternate methods of defining a topology in terms of Kuratowski Closure Operator and Neighborhood Systems. Continuous functions and homeomorphism. First and Second Countable spaces. Lindelof's theorems. Separable spaces. Second countability and separability.

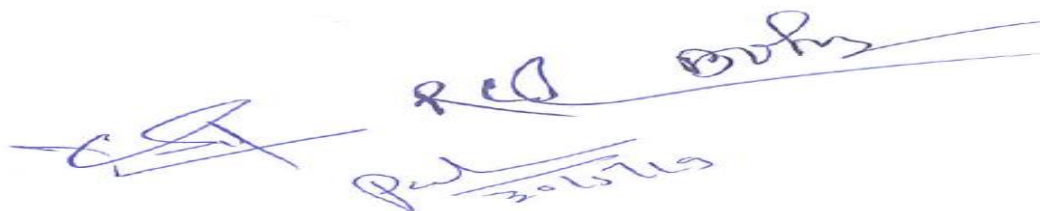
**Unit-III** Separation axioms; their Characterizations and basic properties. Urysohn's lemma, Tietze extension theorem.

**Unit-IV** Compactness. Continuous functions and compact sets. Basic properties of Compactness. Compactness and finite intersection property. Sequentially and countably compact sets. Local compactness and one point compactification. Stone-Cech compactification.

**Unit-V** Compactness in metric spaces. Equivalence of compactness, countable compactness and sequential compactness in metric space. Connected spaces. Connectedness on the real line. Components. Locally connected spaces.

#### Recommended Books:

1. James R. Munkres, Topology, A First Course, Prentice Hall of India Pvt. Ltd., New Delhi, 2000.
2. K. D. Joshi, Introduction to General Topology, Wiley Eastern Ltd., 1983.



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## References

1. J. Dugundji, Topology, Allyn and Bacon, 1966 (reprinted in India by Prentice Hall of India Pvt. Ltd.).
2. George F. Simmons, Introduction to Topology and modern Analysis, McGraw-Hill Book Company, 1963.
3. J. Hocking and G Young, Topology, Addison-Wiley Reading, 1961.
4. J. L. Kelley, General Topology, Van Nostrand, Reinhold Co., New York, 1955.
5. L. Steen and J. Seebach, Counter examples in Topology, Holt, Rinehart and Winston, New York, 1970.
6. W. Thron, Topologically Structures, Holt, Rinehart and Winston, New York, 1966.
7. N. Bourbaki, General Topology Part I (Transl.), Addison Wesley, Reading, 1966.
8. R. Engelking, General Topology, Polish Scientific Publishers, Warszawa, 1977.
9. W. J. Pervin, Foundations of General Topology, Academic Press Inc. New York, 1964.
10. E. H. Spanier, Algebraic Topology, McGraw-Hill, New York, 1966.
11. S. Willard, General Topology, Addison-Wesley, Reading, 1970.
12. Crump W. Baker, Introduction to Topology, Wm C. Brown Publisher, 1991.
13. Sze-Tsen Hu, Elements of General Topology, Holden-Day, Inc. 1965.
14. D. Bushaw, Elements of General Topology, John Wiley & Sons, New York, 1963.
15. M. J. Mansfield, Introduction to Topology, D. Van Nostrand Co. Inc. Princeton, N. J., 1963.
16. B. Mendelson, Introduction to Topology, Allyn & Bacon, Inc., Boston, 1962.
17. C. Berge, Topological Spaces, Macmillan Company, New York, 1963.
18. S. S. Coirns, Introductory Topology, Ronald Press, New York, 1961.
19. Z. P. Mamuzic, Introduction to General Topology, P. Noordhoff Ltd., Groningen, 1963.
20. K. K. Jha, Advanced General Topology, Nav Bharat Prakashan, Delhi.



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**M.Sc./M.A. Course (First Semester)**  
**PAPER-IV**

**Complex Analysis (I)**

Max. Marks 80

**Unit-I** Complex integration, Cauchy-Goursat. Theorem. Cauchy's integral formula. Higher order derivatives. Morera's Theorem. Cauchy's inequality and Liouville's theorem. The fundamental theorem of algebra. Taylor's theorem. Laurent's series. Isolated singularities. Meromorphic functions.

**Unit-II** Maximum modulus principle. Schwarz lemma. The argument principle. Rouché's theorem Inverse function theorem.

**Unit-III** Residues. Cauchy's residue theorem. Evaluation of integrals. Branches of many valued functions with special reference to  $\arg z$ ,  $\log z$  and  $z^a$ .

**Unit-IV** Definitions and examples of conformal mapping Bilinear transformations, their properties and classifications.

**Unit-V** Spaces of analytic functions. Hurwitz's theorem. Montel's theorem Riemann mapping theorem.

**Recommended Books:**

1. Complex Analysis by L.V.Ahlfors, McGraw - Hill, 1979.
2. J. B. Conway, Functions of one Complex variable, Springer-Verlag, International student-Edition, Narosa Publishing House, 1980.

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## References

1. H. A. Priestly, Introduction to Complex Analysis, Clarendon Press, Oxford 1990.
2. Complex Function Theory By D.Sarason
3. Liang-shin Hahn & Bernard Epstein, Classical Complex Analysis, Jones and Bartlett Publishers International, London, 1996.
4. S. Lang, Complex Analysis, Addison Wesley, 1977.
5. D. Sarason, Complex Function Theory, Hindustan Book Agency, Delhi, 1994.
6. Mark J. Ablowitz and A.S. Fokas, Complex Variables: Introduction and Applications, Cambridge University press, South Asian Edition, 1998.
7. E. Hille, Analytic Function Theory (2 Vols.) Gonn & Co., 1959.
8. W. H. J. Fuchs, Topics in the Theory of Functions of one Complex Variable, D.Van Nostrand Co., 1967.
9. C. Caratheodory, Theory of Functions (2 Vols.) Chelsea Publishing Company, 1964.
10. M.Heins, Complex Function Theory, Academic Press, 1968.
11. Walter Rudin, Real and Complex Analysis, McGraw-Hill Book Co., 1966.
12. S. Saks and A.Zygmund, Analytic Functions, Monografic Matematyczne, 1952.
13. E. C. Titchmarsh, The Theory of Functions, Oxford University Press, London.
14. W. A. Veech, A Second Course in Complex Analysis, W.A. Benjamin, 1967.
15. S.Ponnusamy, Foundations of Complex Analysis, Narosa Publishing House, 1997.



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**M.Sc./M.A. Course (First Semester)**  
**PAPER-V**  
**Advanced Discrete Mathematics (I)**

Max. Marks 80

- Unit-I** Formal Logic-Statements. Symbolic Representation and Tautologies. Quantifiers, Predicates and Validity. Propositional Logic. Semigroups & Monoids-Definitions and Examples of Semigroups and monoids (including those pertaining to concatenation operation).
- Unit-II** Homomorphism of semigroups and monoids. Congruence relation and Quotient Semigroups. Subsemigroup and submonoids. Direct Products. Basic Homomorphism Theorem.
- Unit-III** Lattices-Lattices as partially ordered sets. Their properties. Lattices as Algebraic Systems. Sublattices, Direct products, and Homomorphisms. Some Special Lattices e.g., Complete, Complemented and Distributive Lattices. Boolean Algebras-Boolean Algebras as Lattices. Various Boolean Identities. The Switching Algebra example. Subalgebras,
- Unit-IV** Direct Products and Homomorphisms. Join-Irreducible elements, Atoms and Minterms. Boolean Forms and Their Equivalence. Minterm Boolean Forms, Sum of Products Canonical Forms. Minimization of Boolean Functions. Applications of Boolean Algebra to Switching Theory (using AND, OR & NOT gates). The Karnaugh Map Method.
- Unit-V** Grammars and Languages-Phrase-Structure Grammars. Rewriting Rules. Derivations. Sentential Forms. Language generated by a Grammar. Regular, Context-Free, and Context Sensitive Grammars and Languages. Regular sets, Regular Expressions and the Pumping Lemma. Kleene's Theorem. Notions of Syntax Analysis, Polish Notations. Conversion of Infix Expressions to Polish Notations. The Reverse Polish Notation.

  
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### Recommended Books:

1. Elements of Discrete Mathematics by C. L. Liu, McGraw-Hill Book Co.
2. J. P. Tremblay & R. Manohar, Discrete Mathematical Structures with Applications to Computer Science, McGraw-Hill Book Co., 1997.

### References

1. J. L. Gersting, Mathematical Structures for Computer Science, (3<sup>rd</sup> edition), Computer Science Press, New York.
2. Seymour Lipschutz, Finite Mathematics (International) edition (1983), McGraw-Hill Book Company, New York.
3. S. Wiitala, Discrete Mathematics-A Unified Approach, McGraw-Hill Book Co.
4. J. E. Hopcroft and J. D. Ullman, Introduction to Automata Theory, Languages & Computation, Narosa Publishing House.
5. C. L. Liu, Elements of Discrete Mathematics, McGraw-Hill Book Co.
6. N. Deo. Graph Theory with Application to Engineering and Computer Sciences. Prentice Hall of India
7. K. L. P. Mishra and N. Chandrashekar, Theory of Computer Science PHI(2002)

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# HEMCHAND YADAV VISHWAVIDYALAYA, DURG (C.G.)

## M.A. /M.Sc. (MATHEMATICS) (Semester-II)

2019-20 & Onward

There shall be five theory papers. Each paper shall have 100 marks.

**Overall tally of marks will be 500.**

Paper	Description	Theory	Sessional	Practical	Total Marks
I	Advanced Abstract Algebra (II)	80	20	-	100
II	Real Analysis (II)	80	20	--	100
III	General and Algebraic Topology	80	20	--	100
IV	Advanced Complex Analysis (II)	80	20	--	100
V	Advanced Discrete Mathematics (II)	80	20	--	100

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# HEMCHAND YADAV VISHWAVIDYALAYA, DURG (C.G.)

## M.Sc. /M.A. Course (Second Semester)

### PAPER-I

## Advanced Abstract Algebra (II)

Max. Marks 80

**Unit-I** Modules - Cyclic modules. Simple modules. Semi-simple modules. Schuler's Lemma. Free modules. Noetherian and Artinian modules and rings-Hilbert basis theorem. Wedderburn Artin theorem. Uniform modules, primary modules, and Noether-Lasker theorem.

**Unit-II** Linear Transformations - Algebra of linear transformation, Singular and non singular transformation, characteristic roots and vectors, matrices and linear transformations.

**Unit-III** Canonical Forms - Similarity of linear transformations. Invariant subspaces. Reduction to triangular forms. Nilpotent transformations. Index of nilpotency. Invariants of a nilpotent transformation. The primary decomposition theorem. Jordan blocks and Jordan forms.

**Unit-IV** Smith normal form over a principal ideal domain and rank. Fundamental structure theorem for finitely generated modules over a Principal ideal domain and its applications to finitely generated abelian groups.

**Unit-V** Rational canonical form. Generalised Jordan form over any field.

### Books Recommended:

1. P. B. Bhattacharya, S.K.Jain, S.R.Nagpaul : Basic Abstract Algebra, Cambridge University press
2. I. N. Herstein : Topics in Algebra, Wiley Eastern Ltd.
3. Qazi Zameeruddin and Surjeet Singh : Modern Algebra



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## References

1. M. Artin, Algebra, Prentice -Hall of India, 1991.
2. P. M. Cohn, Algebra, Vols. I, II & III, John Wiley & Sons, 1982, 1989, 1991.
3. N. Jacobson, Basic Algebra, Vols. I & II, W. H. Freeman, 1980 (also published by Hindustan Publishing Company).
4. S. Lang, Algebra, 3rd edition, Addison-Wesley, 1993.
5. I. S. Luther and I.B.S. Passi, Algebra, Vol. I-Groups, Vol. II-Rings, Narosa Publishing House (Vol. I-1996, Vol. II-1999)
6. D. S. Malik, J.N. Mordeson, and M.K. Sen, Fundamentals of Abstract Algebra, Mc Graw-Hill, International Edition, 1997.
7. K. B. Datta, Matrix and Linear Algebra, Prentice Hall of India Pvt. Ltd., New Delhi, 2000.
8. S. K. Jain, A. Gunawardena and P.B Bhattacharya, Basic Linear Algebra with MATLAB, Key College Publishing (Springer-Verlag), 2001.
9. S. Kumaresan, Linear Algebra, A Geometric Approach, Prentice-Hall of India, 2000.
10. Vivek Sahai and Vikas Bist, Algebra, Narosa Publishing House, 1999.
11. I. Stewart, Galois Theory, 2nd edition, Chapman and Hall, 1989.
12. J. P. Escofier, Galois Theory, GTM Vol. 204, Springer, 2001.
13. T. Y. Lam, Lectures on Modules and Rings, GTM Vol. 189, Springer-Verlag, 1999.
14. D. S. Passman, A Course in Ring Theory, Wadsworth and Brooks/Cole Advanced Books and Softwares, Pacific groves. California, 1991.
15. Fraleigh, A first course in Algebra Algebra, Narosa, 1982.



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**M.Sc./M.A. Course (Second Semester)**  
**PAPER-II**

**Real Analysis (II)**

Max. Marks 80

- Unit-I** Definition and existence of Riemann-Stieltjes integral, Properties of the Integral, integration and differentiation, the fundamental theorem of Calculus, integration of vector-valued functions, Rectifiable curves.
- Unit-II** Lebesgue outer measure. Measurable sets. Regularity. Measurable functions. Borel and Lebesgue measurability. Non-measurable sets. Integration of Non-negative functions. The General integral. Integration of Series.
- Unit-III** Measures and outer measures, Extension of a measure. Uniqueness of Extension. Completion of a measure. Measure spaces. Integration with respect to a measure. Riemann and Lebesgue Integrals.
- Unit-IV** The Four derivatives. Lebesgue Differentiation Theorem. Differentiation and Integration.
- Unit-V** Functions of Bounded variation. The  $L^p$ -spaces. Convex functions. Jensen's inequality. Holder and Minkowski inequalities. Completeness of  $L^p$ , Convergence in Measure, Almost uniform convergence.

**Recommended Books:**

1. Principle of Mathematical Analysis by W. Rudin
2. Real Analysis by H. L. Roydon

  
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## References

1. T. M. Apostol, Mathematical Analysis, Narosa Publishing House, New Delhi, 1985.
2. Gabriel Klambauer, Mathematical Analysis, Marcel Dekkar, Inc. New York, 1975.
3. A. J. White, Real Analysis; an introduction, Addison-Wesley Publishing Co., Inc., 1968.
4. G. de Barra, Measure Theory and Integration, Wiley Eastern Limited, 1981.
5. E. Hewitt and K. Stromberg. Real and Abstract Analysis, Berlin, Springer, 1969.
6. P. K. Jain and V.P. Gupta, Lebesgue Measure and Integration, New Age International (P) Limited Published, New Delhi, 1986 Reprint 2000).
7. I. P. Natanson, Theory of Functions of a Real Variable. Vol. 1, Frederick Ungar Publishing Co., 1961.
9. Richard L. Wheeden and Antoni Zygmund, Measure and Integral: An Introduction to Real Analysis, Marcel Dekker Inc. 1977.
10. J. H. Williamson, Lebesgue Integration, Holt Rinehart and Winston, Inc. New York. 1962.
11. A. Friedman, Foundations of Modern Analysis, Holt, Rinehart and Winston, Inc., New York, 1970.
12. P. R. Halmos, Measure Theory, Van Nostrand, Princeton, 1950.
13. T. G. Hawkins, Lebesgue's Theory, of Integration: Its Origins and Development, Chelsea, New York, 1979.
14. K. R. Parthasarathy, Introduction to Probability and Measure, Macmillan Company of India Ltd., Delhi, 1977.
15. R.G. Bartle, The Elements of Integration, John Wiley & Sons, Inc. New York, 1966.
16. Serge Lang, Analysis I & II, Addison-Wesley Publishing Company, Inc. 1969.
17. Inder K. Rana, An Introduction to Measure and Integration, Norosa Publishing House, Delhi, 1997.



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**M.Sc./M.A. Course (Second Semester)**  
**PAPER-III**

**General and Algebraic Topology**

Max. Marks 80

- Unit-I** Tychonoff product topology in terms of standard sub-base and its characterizations. Projection maps.
- Unit-II** Product spaces, separation axioms connectedness (Tychonoff's theorem). Compactness, product spaces Countability in product spaces.
- Unit-III** Embedding and metrization. Embedding lemma and Tychonoff embedding. The Urysohn metrization theorem. Metrization theorems and Paracompactness-Local finiteness. The Nagata-Smirnov metrization theorem. Paracompactness. The Smirnov metrization theorem.
- Unit-IV** Nets and filter. Topology and convergence of nets. Hausdorffness and nets. Compactness and nets. Filters and their convergence. Canonical way of converting nets to filters and vice-versa. Ultra-filters and Compactness.
- Unit-V** The fundamental group and covering spaces-Homotopy of paths. The fundamental group. Covering spaces. The fundamental group of the circle and the fundamental theorem of algebra.

**Recommended Books:**

1. James R. Munkres, Topology, A First Course, Prentice Hall of India Pvt. Ltd., New Delhi, 2000.
2. K. D. Joshi, Introduction to General Topology, Wiley Eastern Ltd., 1983.

  
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## References

1. J. Dugundji, Topology, Allyn and Bacon, 1966 (reprinted in India by Prentice Hall of India Pvt. Ltd.).
2. George F. Simmons, Introduction to Topology and modern Analysis, McGraw-Hill Book Company, 1963.
3. J. Hocking and G Young, Topology, Addison-Wiley Reading, 1961.
4. J. L. Kelley, General Topology, Van Nostrand, Reinhold Co., New York, 1955.
5. L. Steen and J. Seebach, Counter examples in Topology, Holt, Rinehart and Winston, New York, 1970.
6. W. Thron, Topologically Structures, Holt, Rinehart and Winston, New York, 1966.
7. N. Bourbaki, General Topology Part I (Transl.), Addison Wesley, Reading, 1966.
8. R. Engelking, General Topology, Polish Scientific Publishers, Warszawa, 1977.
9. W. J. Pervin, Foundations of General Topology, Academic Press Inc. New York, 1964.
10. E. H. Spanier, Algebraic Topology, McGraw-Hill, New York, 1966.
11. S. Willard, General Topology, Addison-Wesley, Reading, 1970.
12. Crump W. Baker, Introduction to Topology, Wm C. Brown Publisher, 1991.
13. Sze-Tsen Hu, Elements of General Topology, Holden-Day, Inc. 1965.
14. D. Bushaw, Elements of General Topology, John Wiley & Sons, New York, 1963.
15. M. J. Mansfield, Introduction to Topology, D. Van Nostrand Co. Inc. Princeton, N.J., 1963.
16. B. Mendelson, Introduction to Topology, Allyn & Bacon, Inc., Boston, 1962.
17. C. Berge, Topological Spaces, Macmillan Company, New York, 1963.
18. S. S. Coirns, Introductory Topology, Ronald Press, New York, 1961.
19. Z. P. Mamuzic, Introduction to General Topology, P. Noordhoff Ltd., Groningen, 1963.
20. K. K. Jha, Advanced General Topology, Nav Bharat Prakashan, Delhi.



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**M.Sc./M.A. Course (Second Semester)**  
**PAPER-IV**

**Advanced Complex Analysis (II)**

Max. Marks 80

**Unit-I** Weierstrass' factorisation theorem. Gamma function and its properties. Riemann Zeta function. Riemann's functional equation. Runge's theorem. Mittag-Leffler's theorem.

**Unit-II** Analytic Continuation. Uniqueness of direct analytic continuation. Uniqueness of analytic continuation along a curve. Power series method of analytic continuation Schwarz Reflection Principle. Monodromy theorem and its consequences.

**Unit-III** Harmonic functions on a disk. Harnack's inequality and theorem. Dirichlet Problem. Green's function.

**Unit-IV** Canonical products. Jensen's formula. Poisson-Jensen formula. Hadamard's three circles theorem. Order of an entire function. Exponent of Convergence. Borel's theorem. Hadamard's factorization theorem.

**Unit-V** The range of an analytic function. Bloch's theorem. The Little Picard theorem. Schottky's theorem. Montel Caratheodory and The Great Picard theorem. Univalent functions. Bieberbach's conjecture (Statement only) and the "1/4-theorem.

**Recommended Books:**

1. L. V. Ahlfors, Complex Analysis, MCGraw - Hill, 1979.
2. J. B. Conway, Functions of one Complex variable, Springer-Verlag, International student-Edition, Narosa Publishing House, 1980.



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## References

1. H. A. Priestly, Introduction to Complex Analysis, Clarendon Press, Oxford 1990.
2. Liang-shin Hahn & Bernard Epstein, Classical Complex Analysis, Jones and Bartlett Publishers International, London, 1996.
3. S. Lang, Complex Analysis, Addison Wesley, 1977.
4. Mark J. Ablowitz and A.S. Fokas, Complex Variables: Introduction and Applications, Cambridge University press, South Asian Edition, 1998.
5. E. Hille, Analytic Function Theory (2 Vols.) Gonn & Co., 1959.
6. W. H. J. Fuchs, Topics in the Theory of Functions of one Complex Variable, D. Van Nostrand Co., 1967.
7. C. Caratheodory, Theory of Functions (2 Vols.) Chelsea Publishing Company, 1964.
8. M. Heins, Complex Function Theory, Academic Press, 1968.
9. Walter Rudin, Real and Complex Analysis, McGraw-Hill Book Co., 1966.
10. S. Saks and A. Zygmund, Analytic Functions, Monografic Matematyczne, 1952.
11. E.C Titchmarsh, The Theory of Functions, Oxford University Press, London.
12. W. A. Veech, A Second Course in Complex Analysis, W.A. Benjamin, 1967.
13. S. Ponnusamy, Foundations of Complex Analysis, Narosa Publishing House, 1997.
14. D. Sarason, Complex Function Theory, Hindustan Book Agency, Delhi, 1994.

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## M.Sc./M.A. Course (Second Semester)

### PAPER-V

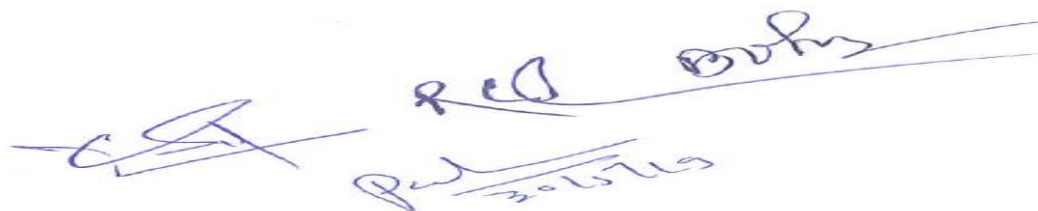
### Advanced Discrete Mathematics (II)

Max. Marks 80

- Unit-I** Graph Theory-Definition of (Undirected) Graphs, Paths, Circuits, Cycles, & Subgraphs. Induced Subgraphs. Degree of a vertex. Connectivity. Planar Graphs and their properties. Trees. Euler's Formula for connected planar Graphs. Complete & Complete Bipartite Graphs. Kuratowski's Theorem (statement only) and its use.
- Unit-II** Spanning Trees, Cut-sets, Fundamental Cut -sets, and Cycle. Minimal Spanning Trees and Kruskal's Algorithm. Matrix Representations of Graphs. Euler's Theorem on the Existence of Eulerian Paths and Circuits.
- Unit-III** Directed Graphs. In degree and Out degree of a Vertex. Weighted undirected Graphs. Dijkstra's Algorithm.. strong Connectivity & Warshall's Algorithm. Directed Trees. Search Trees. Tree Traversals.
- Unit-IV** Introductory Computability Theory-Finite State Machines and their Transition Table Diagrams. Equivalence of finite State Machines. Reduced Machines. Homomorphism.
- Unit-V** Finite Automata. Acceptors. Non-deterministic Finite Automata and equivalence of its power to that of Deterministic Finite Automata. Moore and mealy Machines. Turing Machine and Partial Recursive Functions.

#### Recommended Books:

1. Elements of Discrete Mathematics By C. L. Liu
2. Graph Theory and its application By N. Deo
3. Theory of Computer Science By K. L. P. Mishra and N. Chandrashekar



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## References

1. J. P. Tremblay & R. Manohar, Discrete Mathematical Structures with Applications to Computer Science, McGraw-Hill Book Co., 1997.
2. J. L. Gersting, Mathematical Structures for Computer Science, (3rd edition), Computer Science Press, New York.
3. Seymour Lipschutz, Finite Mathematics (International) edition 1983), McGraw-Hill Book Company, New York.
4. S. Wiitala, Discrete Mathematics-A Unified Approach, McGraw-Hill Book Co.
5. J. E. Hopcroft and J. D. Ullman, Introduction to Automata Theory, Languages & Computation, Narosa Publishing House.
6. C.L Liu, Elements of Discrete Mathematics, McGraw-Hill Book Co.
7. N. Deo. Graph Theory with Application to Engineering and Computer Sciences. Prentice Hall of India.

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# HEMCHAND YADAV VISHWAVIDYALAYA, DURG (C.G.)

## M.A./M.Sc. (MATHEMATICS) (Semester-III) 2020-21 & Onward

There shall be five theory papers. Two compulsory and three optional. Each paper shall have 100 marks. Out of these five papers, the paper which has theory and practical both, the theory part shall have 70 marks and practical part shall have 30 marks. **Overall tally of marks in theory and practical will be 500.**

Paper	Description	Theory	Sessional	Practical	Remark	
<b>Compulsory Papers</b>						
I	Integration Theory and Functional Analysis (I)	80	20	--	--	
II	Partial Differential Equations & Mechanics (I)	80	20	--	--	
<b>Optional Papers</b>						
III	A	Fundamentals of Computer Science ( Object Oriented Programming and Data Structure)	70	--	30	For regular students only
	B	General Relativity and Cosmology (I)	80	20	--	--
	C	Fuzzy Set Theory & Its Applications (I)	80	20	--	--
	D	Mathematical Biology (I)	80	20	--	--
IV	A	Operations Research (I)	80	20	--	--
	B	Wavelets (I)	80	20	--	--
V	A	Programming in C (with ANSI Features) (I)	70	--	30	For regular students only
	B	Graph Theory (I)	80	20	--	--
	C	Algebraic Number Theory (I)	80	20	--	--

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# HEMCHAND YADAV VISHWA VIDYALAYA, DURG (C.G.)

## M.Sc./M.A. Course (Third Semester)

### PAPER -I

#### Integration Theory and Functional Analysis (I)

Max. Marks 80

#### Integration Theory:

**Unit-I** Signed measure. Hahn decomposition theorem, mutually singular measures. Radon-Nikodym theorem. Lebesgue decomposition. Riesz representation theorem. Extension theorem (Caratheodory).

**Unit-II** Lebesgue-Stieltjes integral, product measures, Fubini's theorem. Differentiation and Integration. Decomposition into absolutely continuous and singular parts.

**Unit-III** Baire sets. Baire measure, continuous functions with compact support. Regularity of measures on locally compact spaces. Integration of continuous functions with compact support, Riesz-Markoff theorem.

#### Functional Analysis :

**Unit-IV** Normed linear spaces. Banach spaces and examples. Quotient space of normed linear spaces and its completeness, equivalent norms. Riesz Lemma, basic properties of finite dimensional normed linear spaces and compactness.

**Unit-V** Weak convergence and bounded linear transformations, normed linear spaces of bounded linear transformations, dual spaces with examples.

#### Books Recommended :

1. P. R. Halmos, Measure Theory, Van Nostrand, Princeton, 1950.
2. B. Choudhary and S.Nanda, Functional Analysis with Applications. Wiley Eastern Ltd. 1989.
3. H. L. Royden, Real Analysis, Macmillan Publishing Co. Inc., New York, 4<sup>th</sup> Edition, 1993.



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## References

1. S. K. Berberian, Measure and integration, Chelsea Publishing Company, New York, 1965.
2. G. de Barra, Measure Theory and Integration, Wiley Eastern Limited, 1981.
3. P. K. Jain and V.P. Gupta, Lebesgue Measure and Integration, New Age International (P) Limited, New Delhi, 2000.
4. Richard L. Wheeden and Antoni Zygmund, Measure and Integral : An Introduction to Real Analysis, Marcel Dekker Inc. 1977.
5. J. H. Williamson, Lebesgue Integration, Holt Rinehart and Winston, Inc. New York. 1962.
6. T. G. Hawkins, Lebesgue's Theory of Integration: Its Origins and Development, Chelsea, New York, 1979.
7. K. R. Parthasarathy, Introduction to Probability and Measure, Macmillan Company of India Ltd., Delhi, 1977.
8. R. G. Bartle, The Elements of Integration, John Wiley & Sons, Inc. New York, 1966.
9. Serge Lang, Analysis I & II, Addison-Wesley Publishing Company, Inc. 1967.
10. Inder K. Rana, An Introduction to Measure and Integration, Narosa Publishing House, Delhi, 1997.
11. Walter Rudin, Real & Complex Analysis, Tata McGraw-Hill Publishing.
12. Edwin Hewitt and Korl Stromberg, Real and Abstract Analysis, Springer-Verlag, New York.
13. Edwin Hewitt and Kenneth A. Ross, Abstract Harmonic Analysis, Vol. 1, Springer-Verlag, 1993.
14. G. Bachman and L. Narici, Functional Analysis, Academic Press, 1966.
15. N. Dunford and J.T. Schwartz, Linear Operators, Part I, Interscience, New York, 1958.
16. R. E. Edwards, Functional Analysis, Holt Rinehart and Winston, New York, 1965.
17. C. Goffman and G. Pedrick, First Course in Functional Analysis, Prentice Hall of India, New Delhi, 1987.
18. P. K. Jain, O.P. Ahuja and Khalil Ahmad, Functional Analysis, New Age International (P) Ltd. & Wiley Eastern Ltd., New Delhi, 1997.
19. R. B. Holmes, Geometric Functional Analysis and its Applications, Springer-Verlag, 1975.
20. K.K. Jha, Functional Analysis, Students' Friends, 1986.
21. L. V. Kantorovich and G.P. Akilov, Functional Analysis, Pergamon Press, 1982.
22. E. Kreyszig, Introductory Functional Analysis with Applications, John Wiley & Sons, New York, 1978.
23. B. K. Lahiri, Elements of Functional Analysis, The World Press Pvt. Ltd., Calcutta, 1994.
24. A. H. Siddiqui, Functional Analysis with Applications, Tata McGraw-Hill Publishing Company Ltd. New Delhi



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25. B. V. Limaye, Functional Analysis, Wiley Eastern Ltd.
26. L. A. Lustenik and V.J. Sobolev, Elements of Functional Analysis, Hindustan Publishing Corporation, New Delhi, 1971.
27. G. F. Simmons, Introduction to Topology and Modern Analysis, McGraw-Hill Book Company, New York, 1963.
28. A. E. Taylor, Introduction to Functional Analysis, John Wiley and Sons, New York, 1958.
29. K. Yosida, Functional Analysis, 3<sup>rd</sup> edition Springer-Verlag, New York, 1971.
30. J. B. Conway, A Course in Functional Analysis, Springer-Verlag, New York, 1990.
31. Walter Rudin, Functional Analysis, Tata McGraw-Hill Publishing Company Ltd., New Delhi, 1973.
32. A. Wilansky, Functional Analysis, Blaisdell Publishing Co., 1964.
33. J. Tinsley Oden & Leszek F. Dernkowicz, Applied Functional Analysis, CRC Press Inc., 1996.

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**M.Sc./M.A. Course (Third Semester)**  
**PAPER -II**  
**Partial Differential Equations and Mechanics (I)**

Max. Marks 80

**Partial Differential Equations**

**Unit-I** Examples of PDE. Classification. Transport Equation-Initial value Problem. Non-homogeneous Equation, Laplace's Equation-Fundamental Solution, Mean Value Formulas, Properties of Harmonic Functions, Green's Function, Energy Methods.

**Unit-II** Heat Equation-Fundamental Solution, Mean Value Formula, Properties of Solutions, Energy Methods. Wave Equation-Solution by Spherical Means, Non-homogeneous Equations, Energy Methods.

**Analytical Dynamics:**

**Unit-III** Generalized coordinates. Holonomic and Non-holonomic systems. Scleronomic and Rheonomic systems. Generalized potential. Lagrange's equations of first kind. Lagrange's equations of second kind. Uniqueness of solution. Energy equation for conservative fields. Hamilton's variables. Donkin's theorem. Hamilton canonical equations. Cyclic coordinates. Routh's equations.

**Unit-IV** Poisson's Bracket. Poisson's Identity. Jacobi-Poisson Theorem. Motivating problems of calculus of variations, Shortest distance. Minimum surface of revolution. Brachistochrone problem. Isoperimetric problem. Geodesic. Fundamental lemma of calculus of variations. Euler's equation for one dependent function and its generalization to (i) 'n' dependent functions, (ii) higher order derivatives. Conditional extremum under geometric constraints and under integral constraints.

  
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## Gravitation:

**Unit-V** Attraction and potential of rod, disc, spherical shells and sphere.  
Surface integral of normal attraction (application & Gauss' theorem).  
Laplace and Poisson equations. Work done by self attracting systems. Distributions for a given potential. Equipotential surfaces.  
Surface and solid harmonics. Surface density in terms of surface harmonics.

## Books Recommended:

1. L. C. Evans, Partial Differential Equations, Graduate Studies in Mathematics, Volume 19, AMS, 1998.
2. F. Gantmacher, Lectures in Analytic Mechanics, MIR Publishers, Moscow, 1975.
3. R. C. Mondal, Classical Mechanics, Prentice Hall of India
4. S. L. Loney, An Elementary Treatise on Statics, Kalyani Publishers, New Delhi, 1979.

## References

1. Books on Partial differential equation by I.N. Sneddon, F. John, P. Prasad and R. Ravindran, Amarnath etc.
2. A. S. Ramsey, Dynamics Part II, The English Language Book Society and Cambridge University Press, 1972.
3. H. Goldstein, Classical Mechanics (2nd edition), Narosa Publishing House, New Delhi.
4. I. M. Gelfand and S.V. Fomin, Calculus of Variations, Prentice Hall.
5. Narayan Chandra Rana & Pramod Sharad Chandra Joag, Classical Mechanics, Tata McGraw Hill, 1991.
6. Louis N. Hand and Janet D. Finch, Analytical Mechanics, Cambridge University Press, 1998.
7. A. S. Ramsey, Newtonian Gravitation, The English Language Book Society and the Cambridge University Press.



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**M.Sc./M.A. Course (Third Semester)**  
**PAPER-III (A)**  
**Fundamentals of Computer Science-Theory and Practical**  
**(Object Oriented Programming and Data Structure)**

Max. Marks. 100  
(Theory-70 +Practical-30)

- Unit-I** Object Oriented Programming-Classes and Scope, nested classes, pointer class members; Class initialization, assignment and destruction.
- Unit-II** Overloaded functions and operators; Templates including class templates; class inheritance and virtual functions.
- Unit-III** Data Structures-Analysis of algorithms, q, W, 0, o, w notations ; Sequential and linked representations, Lists, Stacks, and queues;
- Unit-IV** Trees: Binary tree- search tree implementation, B-tree (concept only);
- Unit-V** Sorting: Insertion sort, shell sort, quick-sort, heap sort and their analysis; Hashing-open and closed.

**Books Recommended :**

1. S. B. Lipman, J. Lajoi: C++ Primer, Addison Wesley.
2. B. Stroustrup; The C++ Programming Language, Addison Wesley.
3. C. J. Date : Introduction to Database Systems, Addison Wesley.
4. C. Ritehie: Operating Systems-Incorporating UNIX and Windows, BPB Publications.
5. M. A. Weiss, Data Structures and Algorithm Analysis in C++, Addison Wesley.

**Practical Examination Scheme**

Max. Marks – 30	Time Duration – 3 Hrs.
Practical (two)	20 Marks( 10 marks each)
Viva	05 Marks
Sessional	05 Marks



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**M.Sc./M.A. Course (Third Semester)**  
**PAPER-III (B)**  
**General Relativity & Cosmology (I)**

Max Marks – 80

- Unit-I** General Relativity-Transformation of coordinates. Tensors. Algebra of Tensors. Symmetric and skew symmetric Tensors. Contraction of tensors and quotient law. Riemannian metric. Parallel transport. Christoffel Symbols. Covariant derivatives, intrinsic derivatives and geodesics.
- Unit-II** Riemann Christoffel curvature tensor and its symmetry properties. Bianchi identities and Einstein tensor. Review of the special theory of relativity and the Newtonian Theory of gravitation.
- Unit-III** Principle of equivalence and general covariance, geodesic principle, Newtonian approximation of relativistic equations of motion. Einstein's field equations and its Newtonian approximation.
- Unit-IV** Schwarzschild external solution and its isotropic form. Planetary orbits and analogues of Kepler's Laws in general relativity. Advance of perihelion of a planet. Bending of light rays in a gravitational field, gravitational redshift of spectral lines. Radar echo delay.
- Unit-V** Energy-momentum tensor of a perfect fluid. Schwarzschild internal solution. Boundary conditions. Energy momentum tensor of an electromagnetic field. Einstein-Maxwell equations. Reissner-Nordström solution.

  
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## REFERENCES:

1. C. E. Weatherbum, An Introduction to Riemannian Geometry and the tensor Calculus, Cambridge University Press, 1950.
2. H. Stephani, General Relativity: An Introduction to the theory of the gravitational field, Cambridge University Press, 1982.
3. A. S. Eddington, The Mathematical Theory of Relativity, Cambridge University Press, 1965.
4. J. V. Narlikar, General Relativity and Cosmology, The Macmillan Company of India Limited, 1978.
5. R. Adiev, M. Bazin, M. Schiffer, Introduction to general relativity, McGraw Hill Inc., 1975.
6. B. F. Schutz, A first course in general relativity, Cambridge University Press, 1990.
7. S. Weinberg, Gravitation and Cosmology: Principles and applications of the general theory of relativity, John Wiley & Sons, Inc. 1972.
8. R. K. Sachs and H. Wu., General Relativity for Mathematician, Springer Verlag, 1977.
9. J. L. Synge, Relativity: The general theory. North Holland Publishing Company, 1976.

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**M.Sc./M.A. Course (Third Semester)**  
**PAPER-III (C)**  
**Fuzzy Set Theory and Its Applications (I)**

Max Marks – 80

**UNIT-I** Fuzzy sets-Basic definitions,  $\alpha$ -level sets. Convex fuzzy sets. Basic operations on fuzzy sets. Types of fuzzy sets. Cartesian products, Algebraic products. Bounded sum and difference, t-norms and t-conorms.

**UNIT-II** The Extension Principle- The Zadeh's extension principle. Image and inverse image of fuzzy sets. Fuzzy numbers. Elements of fuzzy arithmetic.

**UNIT-III** Fuzzy Relations on Fuzzy sets, Composition of Fuzzy relations. Min-Max composition and its properties.

**UNIT-IV** Fuzzy equivalence relations. Fuzzy compatibility relations. Fuzzy relation equations. Fuzzy graphs, Similarity relation.

**UNIT-V** Possibility Theory-Fuzzy measures. Evidence theory. Necessity measure. Possibility measure. Possibility distribution. Possibility theory and fuzzy sets. Possibility theory versus probability theory.

**REFERENCES :**

1. H. J. Zmmemann, Fuzzy set theory and its Applications, Allied Publishers Ltd. New Delhi, 1991.
2. G. J. Klir and B. Yuan- Fuzzy sets and fuzzy logic, Prentice-Hall of India, New Delhi, 1995.



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**M.Sc./M.A. Course (Third Semester)**  
**PAPER-III (D)**  
**Mathematical Biology (I)**

Max. Marks - 80

**UNIT-I**

**Population Dynamics**

Malthusian growth model, Logistic equation, model of species competition, Linear and Nonlinear First Order Discrete Time Models, Biology of Insect Population Dynamics, Model for Insect Population Dynamics with Competition, Differential Equation Models.

**UNIT-II**

**Age Structured Population Dynamics**

Evolutionary Aspects, Harvesting and Fisheries, Metapopulations, Delay Effects, Fibonacci's Rabbits, golden ratio, Age-structured Population's in Discrete Time, continuous age-structured populations, Euler-Lotka Equations.

**UNIT-III**

**Population Dynamics of Interacting Species**

Host-parasitoid Interactions, Lotka-Volterra Prey-predator Equations, Modelling the Predator Functional Response, Ecosystems Modelling, Interacting Metapopulations, Competition, Predation, Predator-mediated Coexistence of Competitors, Effects of Habitat Destruction.

**UNIT-IV**

**Population Genetics and Evolution**

Mendelian Genetics in Populations with Non-overlapping Generations, Haploid genetics, Spread of a favored allele, Mutation-selection balance, Diploid genetics, Sexual reproduction, Spread of a favored allele, Mutation-selection balance, Heterosis, Frequency-dependent selection, Linkage equilibrium, Random genetic drift, Evolution of the Genetic System.

**UNIT-V**

**Infectious Disease**

Simple Epidemic and SIS Diseases, SIR Epidemics, SIR epidemic disease model, SIR Endemics, SIR endemic disease model, No Disease-related Death, Including Disease-related Death, Vaccination, Evolution of virulence, Vector -borne Diseases, Basic Model for Macroparasitic Diseases.

**Recommended Books**

1. Jeffrey R. Chasnov, Mathematical Biology, Lecture Notes for MATH(365), The Hong Kong University of Science and Technology (2010)
2. Nicholas F. Britton, Essential Mathematical Biology, Springer-Verlag(2003)
3. J.D.Murray, Mathematical Biology I. An Introduction, Springer-Verlag (2002) 3<sup>rd</sup> Edition.
4. J. D. Murray, Mathematical Biology II. Spatial Models and Biomedical Application, Springer-Verlag (2003) 3<sup>rd</sup> Edition.

  
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**M.Sc./M.A. Course (Third Semester)**  
**PAPER -IV (A)**  
**Operations Research (I)**

Max. Marks 80

- Unit-I** Operations Research and its Scope. Necessity of Operations Research in Industry. Linear Programming-Simplex Method. Theory of the Simplex Method. Duality and Sensitivity Analysis.
- Unit-II** Other Algorithms for Linear Programming-Dual Simplex Method.
- Unit-III** Parametric Linear Programming. Upper Bound Technique. Interior Point Algorithm. Linear Goal Programming.
- Unit-IV** Transportation and Assignment Problems.
- Unit-V** Network Analysis-Shortest Path Problem. Minimum Spanning Tree Problem. Maximum Flow Problem. Minimum Cost Flow Problem. Network Simplex Method. Project Planning and Control I with PERT-CPM.

**Books Recommended :**

1. F. S. Hillier and G.J. Ueberman. Introduction to Operations Research (Sixth Edition), McGraw Hill International Edition, Industrial Engineering Series, 1995. (This book comes with a CD containing tutorial software).
2. G. Hadley, Linear Programming, Narosa Publishing House, 1995.
3. G. Hadley, Nonlinear and Dynamic Programming, Addison-Wesley, Reading Mass.
4. H. A. Taha, Operations Research -An introduction, Macmillan Publishing Co., Inc., New York.
5. Kanti Swarup, P.K. Gupta and Man Mohan, Operations Research, Sultan Chand & Sons, New Delhi
6. Mokhtar S. Bazaraa, John J. Jarvis and Hanif D. Sherali, Linear Programming and Network flows, John Wiley & Sons, New York, 1990.

  
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## References

1. S. S. Rao, Optimization Theory and Applications, Wiley Eastern Ltd., New Delhi.
2. Prem Kumar Gupta and D.S. Hira, Operations Research-An Introduction. S. Cliand & Company Ltd., New Delhi.
3. N. S. Kambo, Mathematical Programming Techniques, Affiliated East-West Press Pvt. Ltd., New Delhi, Madras
4. R. K. Rathy, An Introduction to Fluid Dynamics, Oxford and IBH Publishing Company, New Delhi, 1976.
5. A. D. Young, Boundary Layers, AIAA Education Series, Washington DC, 1989.
6. S. W. Yuan, Foundations of Fluid Mechanics, Prentice Hall of India Private Limited, New Delhi, 1976.
7. LINGO Systems Products (Visit websHe <http://www.Hndo.com/productsf.html>)
  - (i) LINGO (the linear programming solver)
  - (ii) LINGO Callable Library (the premier optimisation engine)
  - (iii) LINGO (the linear, non-linear, and integer programming solver with mathematical modelling language)
    - (i) What's Best I (the spreadsheet add-in that solves linear, non- linear, and integer problems).

All the above four products are bundled into one package to form the Solver Suite. For more details about any of the four products one has to click on its name.

- (i) Optimisation Modelling with LINGO (8" edition) by Linus Schrage.
  - (ii) Optimisation Modelling with LINGO by Unus Schrage.
- More details available on the Related Book page York, 1979.



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**M.Sc./M.A. Course (Third Semester)**  
**PAPER-IV (B)**  
**Wavelets (I)**

Max Marks – 80

- Unit-I.** Preliminaries-Different ways of constructing wavelets- Orthonormal bases generated by a single function: the Balian-Low theorem. Smooth projections on  $L^2(\mathbb{R})$ .
- Unit-II.** Local sine and cosine bases and the construction of some wavelets. The unitary folding operators and the smooth projections.
- Unit-III.** Multiresolution analysis and construction of wavelets. Construction of compactly supported wavelets and estimates for its smoothness. Band limited wavelets.
- Unit-IV.** Orthonormality. Completeness. Characterization of Lemarie-Meyer wavelets and some other characterizations. Franklin wavelets and Spline wavelets on the real line.
- Unit-V.** Orthonormal bases of piecewise linear continuous functions for  $L^2(\mathbb{T})$ . Orthonormal bases of periodic splines. Periodization of wavelets defined on the real line.

**REFERENCES:**

1. Eugenic Hernandez and Guido Weiss, A First Course on Wavelets, CRC Press, New York, 1996.
2. C. K. Chui, An Introduction to Wavelets, Academic Press, 1992.
3. I. Daubechies, Ten Lectures on Wavelets, CBS-NSF Regional Conferences in Applied Mathematics, 61, SIAM, I 1992.
4. Y. Meyer, Wavelets, algorithms and applications (Tran.by R.D. Rayan, SIAM, 1993.
5. M. V. Wickerhauser, Adapted wavelet analysis from theory to software, Wellesley, MA, A.K. Peters, 1994.



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**M.Sc./M.A. Course (Third Semester)**  
**PAPER -V (A)**  
**Programming in C (with ANSI features) Theory and Practical (I)**

Max. Marks. 100  
(Theory-70 +Practical-30)

**Unit-I** An overview of programming. Programming language, Classification. C Essentials-Program Development. Functions. Anatomy of a C Function. Variables and Constants. Expressions. Assignment Statements. Formatting Source Files. Continuation Character. The Preprocessor.

**Unit-II** Scalar Data Types-Declarations, Different Types of Integers. Different kinds of Integer Constants. Floating-Point Types. Initialization. Mixing Types. Explicit Conversions-Casts. Enumeration Types. The Void Data Type. Typedefs. Finding the Address of an object. Pointers.

**Unit-III** Control Flow-Conditional Branching. The Switch Statement. Looping. Nested Loops. The break and continue Statements. The goto statement. Infinite Loops.

**Unit-IV** Operators and Expressions-Precedence and Associativity. Unary Plus and Minus operators. Binary Arithmetic Operators. Arithmetic Assignment Operators. Increment and Decrement Operators. Comma Operator. Relational Operators. Logical Operators. Bit - Manipulation Operators. Bitwise Assignment Operators. Cast Operator. Size of Operators. Conditional Operator. Memory Operators.

**Unit-V** Arrays -Declaring an Array. Arrays and Memory. Initializing Arrays. Encryption and Decryption.



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## Books Recommended :

1. Peter A. Darnell and Philip E. Margolis, C: A Software Engineering Approach, Narosa Publishing House (Springer International Student Edition) 1993.
2. Samuel P. Harkison and Gly L. Steele Jr., C : A Reference Manual, 2nd Edition, Prentice Hall, 1984.
3. Brian W. Kernighan & Dennis M. Ritchie, The C Programme Language, 2nd Edition (ANSI Features), Prentice Hall 1989.

## Practical Examination Scheme

Max. Marks – 30

Time Duration – 3 Hrs.

Practical (two)

20 Marks( 10 marks each)

Viva

05 Marks

Sessional

05 Marks

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## M.Sc./M.A. Course (Third Semester)

### PAPER-V (B)

### Graph theory (I)

Max. Marks - 80

Unit-I: Operations on graphs, matrices and vector spaces: Topological operations, Homeomorphism, homomorphism, contractions, derived graphs, Binary operations.

Unit-II: Matrices and vector spaces: Matrices and vector spaces : The adjacency matrix, The determinant and the spectrum, Spectrum properties, The incidence matrix, cycle space and Bond space, Cycle bases and cycle graphs.

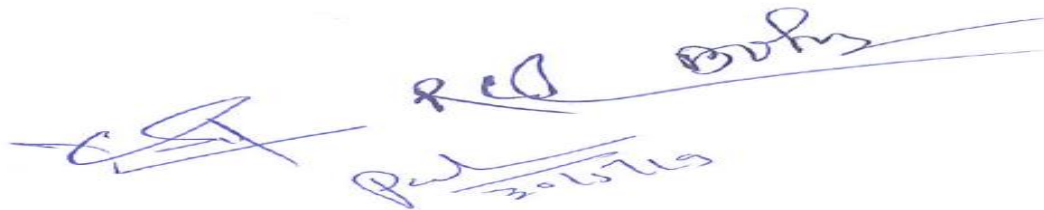
Unit-III: Colouring packing and covering: Vertex coverings, critical graphs, Girth and chromatic number, uniquely colourable graphs, edge-colourings, Face colourings and Beyond, The achromatic and the Adjoint Numbers.

Unit-IV: Combinational formulations: Setting up of combinational formulations, the classic pair of duals, Gallai, Norman-Rabin Theorems, Clique parameters, The Rosenfeld Numbers.

Unit-V: Perfect Graphs: Introduction to the "SPGC", Triangulated (Chordal) graphs, Comparability graphs, Interval graphs, permutation graphs, circular arc graphs, split graphs, weakly triangulated graphs.

### REFERENCES :

1. K. R. Parthasarathy, Basic graph theory, Tata Mc graw Hill publishing company limited , 1994.
2. R. J. Wilson, Introduction to graph theory, Longman Harlow, 1985.
3. John Clark, Derek Allon Holton, A first look at graph Theory, World Scientific Singapore, 1991.
4. Frank Hararary, Graph Theory Narosa, New Delhi, 1995.
5. Ronald Gould and Benjamin Cummins, Graph Theory, California.
6. Narsingh Deo, Graph Theory with applications to Engineering and Computer Science, Prentice-Hall of India Private Limited, New Delhi, 2002.



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**M.Sc./M.A. Course (Third Semester)**  
**PAPER-V (C)**  
**Algebraic Number Theory (I)**

Max Marks – 80

**UNIT-I**

**Elementary Number Theory:** Primes and factorization, Division Algorithm, Congruence, Congruence and Modular Arithmetic, Euler phi function, Primitive roots of Unity, Quadratic law of Reciprocity, Arithmetical functions, Mobius Inversion Formula, The Diophantine Equations, Farey Sequences.

**UNIT-II**

**Algebraic Numbers:** Algebraic Numbers, Conjugates and Discriminants, Algebraic Integers, Integral Bases, Rings of Integers.

**UNIT-III**

**Special Fields:** Calculations for Quadratic fields, cubic fields, biquadratic fields and sextic fields.

**UNIT-IV**

**Localization:** Localization, Integral closure, Prime ideals, Chinese remainder theorem, Galois extensions. **Rings:** Dedekind rings, Discrete valuation rings, Explicit factorization of a prime.

**UNIT-V**

**Completions:** Definitions and completions, Polynomials in complete fields, Structure of complete discrete valuation ring, extension of complete fields.

**References:**

1. Serge Lange: Algebraic Number Theory, Springer-Verlag, 1986.
2. Jean-Pierre Serre: Local Fields, Springer-Verlag, 1979
3. M. Ram Murty, Jody Esmonde: Problems in Algebraic Number Theory (2<sup>nd</sup> ed.), Springer, 2005.
4. H. P. F. Swinnerton-Dyer: A Brief Guide to Algebraic Number Theory, Cambridge University Press, 2001
5. A. Frohlich, M.J. Taylor: Algebraic Number Theory, Cambridge University Press, 1991.
6. Ian Stewart, David Tall : Algebraic Number Theory and Fermat's Last Theorem (3<sup>rd</sup> ed.), A K Peters, Natick, Massachusetts, 2002.
7. Ethan D. Bolker: Elementary Number Theory, An Algebraic Approach, W. A. Benjamin, Inc., New York, 1970
8. Jurgen Neukirch: Algebraic Number Theory, Springer-Verlag, 1999
9. William Stein: Algebraic Number Theory, a Computational Approach, Cambridge University Press, 1991.
10. G. A. Jones and J. M. Jones, Elementary Number Theory, Springer, 1998.



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# HEMCHAND YADAV VISHWAVIDYALAYA, DURG (C.G.)

## Scheme of Examination

### M.A./M.Sc. (MATHEMATICS) (Semester-IV)

#### 2020-21 & Onward

There shall be five papers. Two compulsory and three optional papers. Each paper shall have 100 marks. The paper which has theory and practical both, the theory part shall have 70 marks and practical part shall have 30 marks. **Overall tally of marks in theory and practical will be 500.**

Paper	Description	Theory	Sessional	Practical	Remark	
<b>Compulsory Papers</b>						
I	Functional Analysis (II)	80	20	--	--	
II	Partial Differential Equations & Mechanics	80	20	--	--	
<b>Optional Papers</b>						
III	A	Operating System and Database Management System	70	--	30	For regular students
	B	Cosmology (II)	80	20	--	--
	C	Fuzzy Set Theory & Its Applications	80	20	--	--
	D	Mathematical Biology(II)	80	20	--	--
IV	A	Operations Research (II)	80	20	--	--
	B	Wavelets (II)	80	20	--	--
V	A	Programming in C (with ANSI Features) (II)	70	--	30	For regular students
	B	Graph Theory (II)	80	20	--	
	C	Algebraic Number Theory	80	20	--	

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# HEMCHAND YADAV VISHWA VIDYALAYA, DURG (C.G.)

## M.Sc./M.A. Course (Fourth Semester)

### PAPER -I

### Functional Analysis (II)

Max. Marks 80

**Unit-I** Uniform boundedness theorem and some its consequences. Open mapping and closed graph theorems.

**Unit-II** Hahn-Banach theorem for real linear spaces, complex linear spaces and normed linear spaces. Reflexive spaces. Weak Sequential Compactness. Compact Operators. Solvability of linear equations in Banach spaces. The closed Range Theorem.

**Unit-III** Inner product spaces. Hilbert spaces. Orthonormal Sets. Bessel's inequality. Complete orthonormal sets and Parseval's identity.

**Unit-IV** Structure of Hilbert spaces. Projection theorem. Riesz representation theorem. Adjoint of an operator on a Hilbert space. Reflexivity of Hilbert spaces.

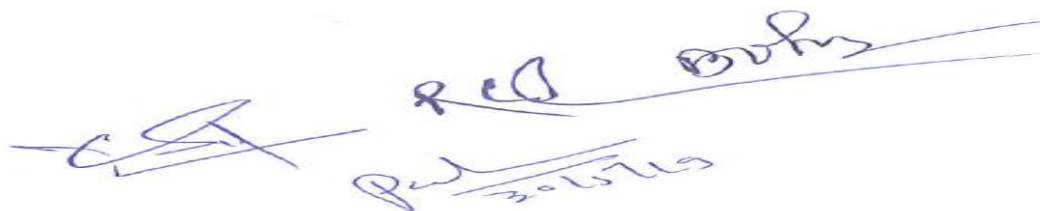
**Unit-V** Self-adjoint operators, Positive, projection, normal and unitary operators. Abstract variational boundary-value problem. The generalized Lax-Milgram theorem.

### Books Recommended :

1. B. Choudhary and S. Nanda, Functional Analysis with Applications. Wiley Eastern Ltd. 1989.
2. H. L. Royden, Real Analysis, Macmillan Publishing Co. Inc., New York, 4th Edition, 1993.

### References

1. Serge Lang, Analysis I & II, Addison-Wesley Publishing Company, Inc. 1967.
2. Walter Rudin, Real & Complex Analysis, Tata McGraw-Hill Publishing.
3. Edwin Hewitt and Karl Stromberg, Real and Abstract Analysis, Springer-Verlag, New York.
4. Edwin Hewitt and Kenneth A. Ross, Abstract Harmonic Analysis, Vol. 1, Springer-Verlag, 1993.



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5. G. Bachman and L. Narici, Functional Analysis, Academic Press, 1966.
6. N. Dunford and J.T. Schwartz, Linear Operators, Part I, Interscience, New York, 1958.
7. R. E. Edwards, Functional Analysis, Holt Rinehart and Winston, New York, 1965.
8. C. Goffman and G. Pedrick, First Course in Functional Analysis, Prentice Hall of India, New Delhi, 1987.
9. P. K. Jain, O.P. Ahuja and Khalil Ahmad, Functional Analysis, New Age International (P) Ltd. & Wiley Eastern Ltd., New Delhi, 1997.
10. R. B. Holmes, Geometric Functional Analysis and its Applications, Springer-Verlag, 1975.
11. K. K. Jha, Functional Analysis, Students' Friends, 1986.
12. L. V. Kantorovich and G.P. Akilov, Functional Analysis, Pergamon Press, 1982.
13. E. Kreyszig, Introductory Functional Analysis with Applications, John Wiley & Sons, New York, 1978.
14. B. K. Lahiri, Elements of Functional Analysis, The World Press Pvt. Ltd., Calcutta, 1994.
15. A. H. Siddiqui, Functional Analysis with Applications, Tata McGraw-Hill Publishing Company Ltd. New Delhi
16. B.V. Limaye, Functional Analysis, Wiley Eastern Ltd.
17. L.A. Lustenik and V.J. Sobolev, Elements of Functional Analysis, Hindustan Publishing Corporation, New Delhi, 1971.
18. G. F. Simmons, Introduction to Topology and Modern Analysis, McGraw-Hill Book Company, New York, 1963.
19. A. E. Taylor, Introduction to Functional Analysis, John Wiley and Sons, New York, 1958.
20. K. Yosida, Functional Analysis, 3<sup>rd</sup> edition Springer-Verlag, New York, 1971.
21. J.B. Conway, A Course in Functional Analysis, Springer-Verlag, New York, 1990.
22. Walter Rudin, Functional Analysis, Tata McGraw-Hill Publishing Company Ltd., New Delhi, 1973.
23. A. Wilansky, Functional Analysis, Blaisdell Publishing Co., 1964.
24. J. Tinsley Oden & Leszek F. Demkowicz, Applied Functional Analysis, CRC Press Inc., 1996.

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**M.Sc./M.A. Course (Fourth Semester)**  
**PAPER -II**  
**Partial Differential Equations and Mechanics (II)**

**Max. Marks 80**

**Partial Differential Equations**

**Unit-I** Non-linear First Order PDE-Complete Integrals, Envelopes, Characteristics, Hamilton Jacobi Equations (Calculus of Variations, Hamilton's ODE, Legendre Transform, Hopf-Lax Formula, Weak Solutions, Uniqueness), Conservation Laws (Shocks, Entropy Condition, Lax Oleinik formula, Weak Solutions, Uniqueness, Riemann's Problem, Long Time Behaviour)

**Unit-II** Representation of Solutions-Separation of Variables, Similarity Solutions (Plane and Travelling Waves, Solitons, Similarity under Scaling), Fourier and Laplace Transform, Hopf-Cole Transform, Hodograph and Legendre Transforms, Potential Functions.

**Unit-III** Asymptotics (Singular Perturbations, Laplace's Method, Geometric Optics, Stationary Phase, Homogenization), Power Series (Non-characteristic Surfaces, Real Analytic Functions, Cauchy-Kovalevskaya Theorem).

**Analytical Dynamics:**

**Unit-IV** Hamilton's Principle. Principle of least action. Poincare Cartan Integral invariant. Whittaker's equations. Jacobi's equations. Lee Hwa Chung's theorem, canonical transformations and properties of generating functions.

  
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**Unit-V** Hamilton-Jacobi equation. Jacobi theorem. Method of separation of variables. Lagrange Brackets. Condition of canonical character of a transformation in terms of Lagrange brackets and Poisson brackets, invariance of Lagrange brackets and Poisson brackets under canonical transformations.

### **Books Recommended :**

1. L. C. Evans, Partial Differential Equations, Graduate Studies in Mathematics, Volume 19, AMS, 1998.
2. F. Gantmacher, Lectures in Analytic Mechanics, MIR Publishers, Moscow, 1975.
3. R. C. Mondal, Classical Mechanics, Prentice Hall of India

### **References**

1. Books on Partial differential equation by IN. Sneddon, F. John, P. Prasad and R. Ravindran, Amarnath etc.
2. A. S. Ramsey, Dynamics Part II, The English Language Book Society and Cambridge University Press, 1972.
3. H. Goldstein, Classical Mechanics (2nd edition), Narosa Publishing House, New Delhi.
4. I. M. Gelfand and S.V. Fomin, Calculus of Variations, Prentice Hall.
5. Narayan Chandra Rana & Pramod Sharad Chandra Joag, Classical Mechanics, Tata McGraw Hill, 1991.
6. Louis N. Hand and Janet D. Finch, Analytical Mechanics, Cambridge University Press, 1998.



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**M.Sc./M.A. Course (Fourth Semester)**  
**PAPER-III (A)**  
**Operating System and Database Management System**  
**- Theory and Practical**

Max. Marks. 100

(Theory-70 +Practical-30)

**Unit-I** Database Systems-Role of database systems, database system architecture and data modeling.

**Unit-II** Introduction to relational algebra and relational calculus.

**Unit-III** Introduction to SQL: Basic features including views; Integrity constraints; Database design-normalization up to BCNF.

**Unit-IV** Operating Systems- Overview of operating system, user interface, processor management, memory management.

**Unit-V** I/O management, concurrency and Security, network and distributed systems.

**Books Recommended :**

1. S. B. Lipman, J. Lajoi: C++ Primer, Addison Wesley.
2. B. Stroustrup; The C++ Programming Language, Addison Wesley.
3. C. J. Date : Introduction to Database Systems, Addison Wesley.
4. C. Ritchie: Operating Systems-Incorporating UNIX and Windows, BPB Publications.
5. M. A. Weiss, Data Structures and Algorithm Analysis in C++, Addison Wesley.

**Practical Examination Scheme**

Max. Marks – 30

Time Duration – 3 Hrs.

Practical (two)


20 Marks( 10 marks each)

Viva

05 Marks

Sessional

05 Marks



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**M.Sc./M.A. Course (Fourth Semester)**  
**PAPER-III (B)**  
**Cosmology (II)**

Max Marks – 80

- Unit-I:** Cosmology-physical universe, Mach's principle, Einstein modified field equations with cosmological term.
- Unit-II:** Static Cosmological models of Einstein and De-Sitter, their derivation, properties and comparison with the actual universe.
- Unit-III:** Hubble's law. Cosmological principles. Weyl's postulate. Derivation of Robertson-Walker metric. Hubble and deceleration parameters. Redshift. Redshift versus distance relation. Angular size versus redshift relation and source counts in Robertson-Walker space-time.
- Unit-IV:** Friedmann models. Fundamental equations of dynamical cosmology. Critical density. Closed and open Universes. Age of the Universe. Matter dominated era of the Universe.
- Unit-V:** Einstein-deSitter model. Particle and event horizons. Eddington-Lemaitre models with  $\Lambda$ -term. Perfect cosmological principle. Steady state cosmology.

**REFERENCES:**

1. J. V. Narlikar, General Relativity and Cosmology The Macmillan Company of India Limited, 1978.
2. S. Weinberg, Gravitation and Cosmology: Principles and applications of the general theory of relativity, John Wiley & Sons, Inc. 1972.
3. J. V. Narlikar, Introduction to Cosmology, Cambridge University Press, 1993.
4. L. D. Landau and E.M. Lifshitz, The classical theory of Fields, Pergamon Press, 1980.

  
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**M.Sc./M.A. Course (Fourth Semester)**  
**PAPER-III (C)**  
**Fuzzy Set Theory & Its Applications (II)**

Max Marks – 80

- Unit-I** Fuzzy Logic-An overview of classical logic, Multivalued logics, Fuzzy propositions. Fuzzy quantifiers. Linguistic variables and hedges. Inference from conditional fuzzy propositions, the compositional rule of inference.
- Unit-II** Approximate Reasoning-An overview of Fuzzy expert system. Fuzzy implications and their selection. Multiconditional approximate reasoning. The role of fuzzy relation equation.
- Unit-III** An introduction to Fuzzy Control-Fuzzy controllers. Fuzzy rule base. Fuzzy inference engine. Fuzzification.
- Unit-IV** Defuzzification and the various defuzzitication methods (the centre of area, the centre of maxima, and the mean of maxima methods).
- Unit-V** Decision Making in Fuzzy Environment-Individual decision making. Multiperson decision making. Multicriteria decision making. Multistage decision making. Fuzzy ranking methods. Fuzzy linear programming.

**REFERENCES :**

1. H. J. Zimmemann, Fuzzy set theory and its Applications, Allied Publishers Ltd. New Delhi, 1991.
2. G. J. Klir and B. Yuan- Fuzzy sets and fuzzy logic, Prentice-Hall of India, New Delhi, 1995.



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# M.Sc./M.A. Course (Fourth Semester)

## PAPER-III (D)

### Mathematical Biology (II)

Max. Marks - 80

#### UNIT-I

**Tumor Modelling:** Phenomenological Models, Nutrients: the Diffusion-limited Stage, Moving Boundary Problems, Growth Promoters and Inhibitors, Vascularisation, Metastasis, Immune System Response.

#### UNIT-II

**Growth and Control of Brain Tumours:** Basic Mathematical Model of Glioma Growth and Invasion, Tumour Spread *In Vitro*: Parameter Estimation, Tumour Invasion in the Rat Brain, Tumour Invasion in the Human Brain, Modelling Tumour Resection in Homogeneous Tissue, Analytical Solution for Tumour Recurrence After Resection, Modelling Surgical Resection with Brain Tissue Heterogeneity, Modelling the Effect of Chemotherapy on Tumour Growth, Modelling Tumour Polyclonality and Cell Mutation.

#### UNIT-III

**Dynamics of Infectious Diseases:** Historical Aside on Epidemics, Simple Epidemic Models and Practical Applications, Modelling Venereal Diseases, Multi-Group Model for Gonorrhoea and Its Control, Bovine Tuberculosis Infection in Badgers and Cattle, Modelling Control Strategies for Bovine Tuberculosis in Badgers and Cattle.

#### UNIT-IV

**Modelling of Immunodeficiency Virus:** AIDS: Modelling the Transmission Dynamics of the Human Immunodeficiency Virus (HIV), HIV: Modelling Combination Drug Therapy, Delay Model for HIV Infection with Drug Therapy, Modelling the Population Dynamics of Acquired Immunity to Parasite Infection, Age- Dependent Epidemic Model and Threshold Criterion, Simple Drug Use Epidemic Model and Threshold Analysis.

#### UNIT-V

**Geographic Spread and Control of Epidemics:** Simple Model for the Spatial Spread of an Epidemic, Spread of the Black Death in Europe, Brief History of Rabies, Spatial Spread of Rabies Among Foxes: Background and Simple Model, Three- Species (*SIR*) Model. Control Strategy Based on Wave Propagation into a Non-epidemic Region: Estimate of Width of a Rabies Barrier, Analytic Approximation for the Width of the Rabies, Effect of Fox Immunity on the Spatial Spread of Rabies.



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### **Recommended Books**

1. Jeffrey R. Chasnov, Mathematical Biology, Lecture Notes for MATH(365), The Hong Kong University of Science and Technology (2010)
2. Nicholas F. Britton, Essential Mathematical Biology, Springer-Verlag(2003)
3. J. D. Murray, Mathematical Biology I. An Introduction, Springer-Verlag (2002) 3<sup>rd</sup> Edition.
4. J. D. Murray, Mathematical Biology II. Spatial Models and Biomedical Application, Springer-Verlag (2003) 3<sup>rd</sup> Edition.

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## M.Sc./M.A. Course (Fourth Semester)

### PAPER -IV (A)

### Operations Research (II)

Max. Marks 80

**Unit-I** Dynamic Programming-Deterministic and Probabilistic Dynamic programming.

**Unit-II** Game Theory-Two-Person, Zero-Sum Games. Games with Mixed Strategies. Graphical . Solution. Solution by Linear Programming.

**Unit-III** Integer Programming-Branch and Bound Technique.

**Unit-IV** Applications to Industrial Problems-Optimal product mix and activity levels. Petroleum, Refinery operations, Blending problems, Economic interpretation of dual linear programming. Problems, Input-output analysis. Leontief system. Indecomposable and Decomposable economies.

**Unit-V** Nonlinear Programming-One/and Multi-Variable Unconstrained Optimization., Kuhn-Tucker Conditions for Constrained Optimization. Quadratic Programming. Separable Programming. I Convex Programming. Non-convex Programming.

### Books Recommended :

1. F. S. Hillier and G. J. Lieberman. Introduction to Operations Research (Sixth Edition), McGraw Hill International Edition, Industrial Engineering Series, 1995. (This book comes with a CD containing tutorial software).
2. G. Hadley, Linear Programming, Narosa Publishing House, 1995.
3. G. Hadly, Nonlinear and Dynamic Programming, Addison-Wesley, Reading Mass.
4. H. A. Taha, Operations Research -An introduction, Macmillan Publishing Co., Inc., New York.
5. Kanti Swarup, P.K. Gupta and Man Mohan, Operations Research, Sultan Chand & Sons, New Delhi
6. Mokhtar S. Bazaraa, John J. Jarvis and Hanif D. Sherali, Linear Programming and Network flows, John Wiley & Sons, New York, 1990.



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## References

1. S. S. Rao, Optimization Theory and Applications, Wiley Eastern Ltd., New Delhi.
2. Prem Kumar Gupta and D.S. Hira, Operations Research-An Introduction. S. Cliand & Company Ltd., New Delhi.
3. N. S. Kambo, Mathematical Programming Techniques, Affiliated East-West Press Pvt. Ltd., New Delhi, Madras
4. R. K. Rathy, An Introduction to Fluid Dynamics, Oxford and IBH Publishing Company, New Delhi, 1976.
5. A. D. Young, Boundary Layers, AIAA Education Series, Washington DC, 1989.
6. S. W. Yuan, Foundations of Fluid Mechanics, Prentice Hall of India Private Limited, New Delhi, 1976.
7. LINDO Systems Products (Visit websHe <http://www.Hndo.com/productsf.html>)
  - (i) LINDO (the linear programming solver)
  - (ii) LINDO Callable Library (the premier optimisation engine)
  - (iii) LINGO (the linear, non-linear, and integer programming solver with mathematical modelling language)
    - (i) What's Best! (the spreadsheets add-in that solves linear, non-linear, and integer problems).

All the above four products are bundled into one package to form the Solver Suite. For more details about any of the four products one has to click on its name.

- (i) Optimisation Modelling with LINDO (8" edition) by Linus Schrage.
- (ii) Optimisation Modelling with LINGO by Linus Schrage. More details available on the Related Book page York, 1979.



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**M.Sc./M.A. Course (Fourth Semester)**

**PAPER-IV (B)**

**Wavelets (II)**

Max Marks – 80

**Unit-I** Characterizations in the theory of wavelets-The basic equations and some of its applications.

**Unit-II** Characterizations of MRA wavelets, low-pass filters and scaling functions. Non-existence of smooth wavelets in  $H^2(\mathbb{R})$ .

**Unit-III Frames** - The reconstruction formula and the Balian-Low theorem for frames. Frames from translations and dilations. Smooth frames for  $H^2(\mathbb{R})$ .

**Unit-IV Discrete** transforms and algorithms-The discrete and the fast Fourier transforms. The discrete and the fast cosine transforms.

**Unit-IV** The discrete version of the local sine and cosine bases. Decomposition and reconstruction algorithms for wavelets.

**REFERENCES:**

1. Eugenic Hernandez and Guido Weiss, A First Course on Wavelets, CRC Press, New York, 1996.
2. C. K. Chui, An Introduction to Wavelets, Academic Press, 1992.
3. I. Daubechies, Ten Lectures on Wavelets, CBS-NSF Regional Conferences in Applied Mathematics, 61, SIAM, I 1992.
4. Y. Meyer, Wavelets, algorithms and applications (Tran. by R.D. Rayan, SIAM, 1993.
5. M. V. Wickerhauser, Adapted wavelet analysis from theory to software, Wellesley, MA, A.K. Peters, 1994.



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**M.Sc./M.A. Course (Fourth Semester)**  
**PAPER -V (A)**  
**Programming in C (with ANSI features)**  
**(II) Theory and Practical**

**Max. Marks. 100**

(Theory-70 +Practical-30)

**Unit-I** Storage Classes-Fixed vs. Automatic Duration. Scope. Global variables. The register Specifier. ANSI rules for the syntax and Semantics of the storage-class keywords.

**Unit-II** Pointers Pointer Arithmetic. Passing Pointers as Function Arguments. Accessing Array Elements through Pointers. Passing Arrays as Function Arguments. Sorting Algorithms. Strings. Multidimensional Arrays. Arrays of Pointers. Pointers to Pointers.

**Unit-III** Functions-Passing Arguments. Declarations and Calls. Pointers to Functions. Recursion. The main Function. Complex Declarations.The C Preprocessor-Macro Substitution. Conditional Compilation. Include Facility. Line Control.

**Unit-IV** Structures and Unions-Structures. Dynamic Memory Allocation. Linked Lists. Unions, enum Declarations.

**Unit-V** Input and Output-Streams, Buffering. The <Stdio.h> Header File. Error Handling. Opening and Closing a File. Reading and Writing Data. Selecting an I/O Method. Unbuffered I/O Random Access. The standard library for Input/Output.



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### **Books Recommended:**

1. Peter A. Darnell and Philip E. Margolis, C: A Software Engineering Approach, Narosa Publishing House (Springer International Student Edition) 1993.
2. Samuel P. Harkison and Gly L. Steele Jr., C : A Reference Manual, 2nd Edition, Prentice Hall, 1984.
3. Brian W. Kernighan & Dennis M. Ritchie, The C Programme Language, 2nd Edition (ANSI Features), Prentice Hall 1989.

### **Practical Examination Scheme**

Max. Marks – 30

Practical (two)

Viva

Sessional

Time Duration – 3 Hrs.

20 Marks( 10 marks each)

05 Marks

05 Marks

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## M.Sc./M.A. Course (Fourth Semester)

### PAPER-V (B)

### Graph theory-II

Max. Marks - 80

Unit-I: Ramsey Theory: Perfectness-preserving operations, Forbidden Subgraph orientations, Ramsey numbers and Ramsey graphs.

Unit-II: Groups: Permutation groups, The automorphism group, graphs with given group, symmetry concepts, pseudo-similarity and stability, spectral studies of the Automorphism group.

Unit-III: Polynomials and Graph Enumeration: The colour polynomials, The chromatic polynomial, The bivariate colouring polynomials.

Unit-IV: Graph Enumeration: Co-chromatic (co-dichromatic) graphs and chromatically unique graphs, Graph Enumeration.

Unit-V: Digraphs & Networks: Digraphs, Types of connectedness, Flows in Networks, Menger's and Konig's Theorem, Degree sequences.

### REFERENCES:

1. K. R. Parthasarathy, Basic graph theory, Tata Mc graw Hill publishing company limited, 1994.
2. R. J. Wilson, Introduction to graph theory, Longman Harlow, 1985.
3. John Clark, Derek Allon Holton, A first look at graph Theory, World Scientific Singapore, 1991.
4. Frank Hararary, Graph Theory Narosa, New Delhi, 1995.
5. Ronald Gould and Benjamin Cummins, Graph Theory, California.
6. Narsingh Deo, Graph Theory with applications to Engineering and Computer Science, Prentice-Hall of India Private Limited, New Delhi, 2002.



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# M.Sc./M.A. Course (Fourth Semester)

## PAPER-V (C)

### Algebraic Number Theory (II)

Max Marks – 80

#### UNIT-I

**Extensions:** Decomposition and ramification, Unramified extensions, Tamely ramified extensions.

#### UNIT-II

**The Different and Discriminant:** Complementary modules, The different and ramification, The discriminant.

#### UNIT-III

**Cyclotomic Fields):** Roots of unity, Quadratic fields, Gauss sums, Relations in ideal classes, Fermat's last theorem.

#### UNIT-IV

**The Structure of Units:** Dirichlet's Unit Theorem, Units in Real Quadratic Fields, Pell's equation.

#### UNIT-V

**Zeta Functions:** The Riemann Zeta Function, Dedekind Zeta Function

#### References:

1. Serge Lang: Algebraic Number Theory, Springer-Verlag, 1986.
2. Jean-Pierre Serre: Local Fields, Springer-Verlag, 1979
3. M. Ram Murty, Jody Esmonde: Problems in Algebraic Number Theory (2<sup>nd</sup> ed.), Springer, 2005.
4. H. P. F. Swinnerton-Dyer: A Brief Guide to Algebraic Number Theory, Cambridge University Press, 2001
5. A. Frohlich, M.J. Taylor: Algebraic Number Theory, Cambridge University Press, 1991.
6. Ian Stewart, David Tall: Algebraic Number Theory and Fermat's Last Theorem (3<sup>rd</sup> ed.), A K Peters, Natick, Massachusetts, 2002.
7. Ethan D. Bolker: Elementary Number Theory, An Algebraic Approach, W. A. Benjamin, Inc., New York, 1970
8. Jurgen Neukirch: Algebraic Number Theory, Springer-Verlag, 1999
9. William Stein: Algebraic Number Theory, a Computational Approach, Cambridge University Press, 1991.

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